

2. (50 points) **Arithmetic on an 8-bit processor.** We have a really \$#!tty 8-bit processor that only has an adder and a bit shifter. It has no ability to perform multiplication or division. We need to compute $(77_{10} - 22_{10}) \times 2$ using only addition and bit shifts.

(a) (15 points) First we're going to calculate the 2's complement representation of -22 . In the box below, write out the binary representation of $+22$, then take its two's complement. Also convert the binary to hex in the boxes at right.

	Binary	Hex									
+22	<table border="1" style="width: 100%; height: 20px; border-collapse: collapse;"> <tr> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> </tr> </table>									<table border="1" style="width: 100%; height: 40px; border-collapse: collapse;"> <tr> <td style="text-align: center; vertical-align: middle;">0x</td> </tr> </table>	0x
0x											
1's(22)	<table border="1" style="width: 100%; height: 20px; border-collapse: collapse;"> <tr> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> </tr> </table>									<table border="1" style="width: 100%; height: 40px; border-collapse: collapse;"> <tr> <td style="text-align: center; vertical-align: middle;">0x</td> </tr> </table>	0x
0x											
2's(22)	<table border="1" style="width: 100%; height: 20px; border-collapse: collapse;"> <tr> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> </tr> </table>									<table border="1" style="width: 100%; height: 40px; border-collapse: collapse;"> <tr> <td style="text-align: center; vertical-align: middle;">0x</td> </tr> </table>	0x
0x											

(b) (15 points) Now add the two's complement of 22 to 77. The result should be the same as $77-22$.

	Binary	Hex									
2's(22)	<table border="1" style="width: 100%; height: 20px; border-collapse: collapse;"> <tr> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> </tr> </table>									<table border="1" style="width: 100%; height: 40px; border-collapse: collapse;"> <tr> <td style="text-align: center; vertical-align: middle;">0x</td> </tr> </table>	0x
0x											
77_{10}	<table border="1" style="width: 100%; height: 20px; border-collapse: collapse;"> <tr> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> </tr> </table>									<table border="1" style="width: 100%; height: 40px; border-collapse: collapse;"> <tr> <td style="text-align: center; vertical-align: middle;">0x</td> </tr> </table>	0x
0x											
$2's(22) + 77_{10}$	<table border="1" style="width: 100%; height: 20px; border-collapse: collapse;"> <tr> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> </tr> </table>									<table border="1" style="width: 100%; height: 40px; border-collapse: collapse;"> <tr> <td style="text-align: center; vertical-align: middle;">0x</td> </tr> </table>	0x
0x											

(c) (10 points) Now multiply the result of the addition from part 2(b) by 2 using a bit shift.

	Binary	Hex									
$2's(22) + 77_{10} \times 2$	<table border="1" style="width: 100%; height: 20px; border-collapse: collapse;"> <tr> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> <td style="width: 12.5%;"></td> </tr> </table>									<table border="1" style="width: 100%; height: 40px; border-collapse: collapse;"> <tr> <td style="text-align: center; vertical-align: middle;">0x</td> </tr> </table>	0x
0x											

(d) (10 points) Convert the result from part 2(c) to **decimal**.